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IR Spectroscopy of Carboxylate-Passivated Semiconducting Nanocrystals: Simulation and Experiment

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wide range of "tilted-bridge"-type geometries and does not indicate the coexistence of "bridging" and "chelating" binding modes as has been previously assumed. This work illustrates the limitations of empirical spectrum assignment and demonstrates the effectiveness of ML-driven molecular dynamics simulations in reproducing the IR spectra of nanoscopic systems.

■ **INTRODUCTION**

Although quantum-confined colloidal nanocrystals (or quantum dots) possess size-dependent and therefore tunable properties,^{[1](#page-5-0)-[4](#page-5-0)} their optoelectronic as well as chemical characteristics can be strongly influenced by ligands passivating their surfaces.^{[5](#page-5-0),[6](#page-5-0)} Consequently, various ligands have been used, for instance, to shift the positions of the nanocrystal band edges, $7,8$ $7,8$ $7,8$ to enhance their optical absorbance, 9 as well as to ensure the chemical stability of the quantum dots. $10,11$ $10,11$ $10,11$ In recent years, organic ligands have also emerged as attractive energy or charge acceptors in nanocrystal-based optical and electronic devices.^{[12](#page-6-0)−[14](#page-6-0)}

In practice, carboxylate-functionalized ligands are frequently used both during nanocrystal synthesis and in postsynthesis
surface modification.^{[10](#page-5-0),[14](#page-6-0)−[16](#page-6-0)} Such ligands can bind to a nanocrystal surface in different geometries, of which four types (chelate, bridge, tilted-bridge, and monodentate) are usually identified depending on the number and position of metal–oxygen bonds^{[17](#page-6-0)–[19](#page-6-0)} (see Figure 1). These modes of binding are typically investigated using IR spectroscopy as the carboxylate-metal bonding is known to influence the carboxyl stretch frequencies.^{18−[24](#page-6-0)} In particular, the IR line shape as well as the splitting between the symmetric and antisymmetric C− O stretching bands, generally found in the region of approximately 1350–1650 cm^{-1} , is conventionally used to infer the existing binding geometries. A commonly used ruleof-thumb, derived from experimental studies of metal complexes, $25,26$ $25,26$ states that for chelating ligands the splitting between the symmetric and antisymmetric C−O stretch bands,

Figure 1. Schematic illustrations of the four binding modes of carboxylate ligands typically considered in the literature.

Δ, is usually around and below 100 cm[−]¹ , for bridges this splitting is found between 100 and 150 cm[−]¹ , while in monodentate ligands it exceeds 200 cm[−]¹ . Nonetheless, given the presence of relatively broad and overlapping IR bands in

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the experimental spectra of nanocrystals, an unambiguous interpretation of their IR signal is usually not straightforward. Additionally, electronic structure calculations suggest that, in terms of Δ-splitting, the tilted-bridge geometries resemble the bridging ones^{[19](#page-6-0)} and are therefore difficult to resolve experimentally and often not discussed separately.

Previously, 27 we have shown, using a model acetatepassivated PbS nanocrystal, that IR spectra of small quantum dots can be effectively simulated using molecular dynamics (MD) utilizing machine-learned force fields trained on DFT data.^{[28](#page-6-0)−[32](#page-6-0)} This approach^{[33](#page-6-0)} was demonstrated to circumvent issues associated with alternative methods that make use of analytical force fields, 34 DFT harmonic mode analysis, $19,35$ $19,35$ $19,35$ or exceedingly computationally intensive ab initio MD (AIMD) simulations.^{[36](#page-6-0)}

In this work, we focus on lead-rich PbS nanocrystals passivated with butyrate and oleate ligands. The results of IR spectroscopy on oleate-passivated PbS (and closely related PbSe) nanocrystals have been repeatedly discussed in the
literature.^{[18](#page-6-0),[21](#page-6-0)−[23,37](#page-6-0)} Following the work of Cass et al.,¹⁸ it has been generally assumed, primarily due to the broad and highly non-Lorentzian shape of the antisymmetric C−O stretch band, that the observed IR signal indicates coexistence of chelating and bridging oleate geometries. Our earlier simulations of acetate-passivated nanocrystals suggested that chelating geometries should not be observed, in line with prior computa-tional studies of carboxylate-passivated CdSe nanocrystals.^{[17,38](#page-6-0)} However, our use of short acetate ligands in our prior work prohibited us from making a direct comparison with experiment.²⁷ The primary aim of this work is, therefore, to resolve this issue by simulating spectra of PbS nanocrystals capped with longer ligands that can also be used experimentally.

First, based on IR measurements, we demonstrate that oleate and butyrate ligands adopt similar binding geometries on the surface of the nanocrystals, which allows us to use the shorter butyrate ligands in our simulations. A qualitative assignment of the experimental IR peaks is then made by performing a DFT harmonic analysis on a single-ligand toy system. Using a machine-learned force field and a dipole algorithm trained on DFT data, we next simulate an IR spectrum of a more realistic model butyrate-passivated PbS nanocrystal. We find that the experimental spectrum can be successfully reproduced by our simulations, in which no significant amounts of chelating geometries are observed. Instead, the broad and asymmetric spectral bands appear to stem from the wide range of bridge and tilted-bridge geometries accessible at room temperature on a disordered nanocrystal−ligand interface. These findings highlight the uncertainties associated with the empirical interpretation of nanocrystal IR spectra since nontrivial spectral line shapes can be observed even in the presence of only one or two nominal ligand coordination geometries. Our results also demonstrate the capability of DFT-trained machine-learning (ML) algorithms to achieve high accuracy and efficiency, thereby enabling effective modeling of the vibrational spectra of nanoscopic structures.

■ **METHODS**

Experiments. Oleate-passivated PbS nanocrystals were synthesized using the procedure described by Kessler et al.³⁹ Butyrate-passivated nanocrystals were obtained by a subsequent solution ligand exchange, see [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S1.1 for details.

The average size of the nanocrystals was estimated at 2.8 nm based on the position of their first exciton absorption band, $3,40$ $3,40$ see [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S1. As described in detail in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S1.3, Fouriertransform infrared spectroscopy (FTIR) spectra of PbS nanocrystals discussed in the main body of this work were measured on films spin-coated on a $CaF₂$ substrate using hexane solutions of freshly synthesized nanocrystals. Spectra of films of aged nanocrystals and films spin-coated from chloroform solutions are discussed in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S2.2.

Simulations. Unless specified otherwise, all electronic structure calculations were performed using the dispersion-corrected B3LYP-D3 functional,^{[41](#page-6-0)-[43](#page-6-0)} LANL2DZ basis set with corresponding effective core potentials⁴⁴ on Pb, S, and I, and 6-31G* basis on the remaining light atoms. Calculations on the single-ligand toy system were performed using NWChem $7.0.0^{45}$ $7.0.0^{45}$ $7.0.0^{45}$ and those on the larger model system using TeraChem $1.9.46,47$ $1.9.46,47$ $1.9.46,47$ $1.9.46,47$

The force field was trained on both energies and forces using
the DeePMD framework.^{[48](#page-6-0)−[50](#page-7-0)} We used a total of 10,648 geometries of the whole $Pb_{19}S_6(butyrate)_{26}$ model system and the training was performed for 7×10^5 steps with a cutoff of 7 Å. The performance of the ML force field during an MD simulation is examined in detail in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S4. We obtain rootmean-square errors on energy and force components of $RMSE(energy) = 0.61$ meV and $RMSE(force) = 81$ meV/Å, well below the recommended thresholds. The dipole moment algorithm was also trained using the DeePMD framework on the same set of geometries for 7.5×10^5 steps with a cutoff of 8 Å. Its performance during MD simulations is also shown in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S4; we find RMSE on dipole vector components of RMSE(dipole) = 0.51 D corresponding to R^2 = 0.985.

The MD simulations were performed using the Atomic Simulation Environment^{[52](#page-7-0)} interfaced with the DeePMD force field using a time step of 1 fs and, when appropriate, a Langevin thermostat with $\gamma = 4.9 \text{ ps}^{-1}$. The initial geometry for the *NVT* simulation was taken from the training set and thermalized for 0.5 ns prior to the *NVE* simulation, which was performed for 3.5 ns. The memspectrum package was used for Burg's maximum entropy spectra analysis method.⁵³ Frequencies in the calculated spectra were scaled by a factor of 0.96 as appropriate for this choice of functional and basis set.^{[54](#page-7-0)}

Additionally, we also trained ML force field and dipole algorithms using DFT data obtained with a smaller $(6-31G/$ lanl2dz) basis set. As we discuss in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S7, MD simulations based on that level of DFT calculations predict similar distributions of ligand geometries as those based on the larger basis set, but this approach yields a poorer agreement between the experimental and simulated vibrational spectra.

All 3D visualizations were rendered with $\rm \tilde{V}MD.^{55}$ $\rm \tilde{V}MD.^{55}$ $\rm \tilde{V}MD.^{55}$

■ **RESULTS AND DISCUSSION**

Experimental IR Spectra. We begin by comparing the experimental IR spectra of PbS nanocrystals functionalized with butyrate and (frequently used) oleate ligands and demonstrate that the two systems possess very similar distributions of carboxylate binding geometries. This will allow us to consider only the shorter and thus computationally more expedient butyrate ligands in the subsequent simulations.

We performed FTIR measurements on thin films of oleateand butyrate-passivated PbS nanocrystals spin-coated onto $CaF₂$ substrates. The used PbS nanocrystals were roughly 2.8 nm in diameter and are therefore expected to possess

exclusively lead-rich (111) facets.^{[10](#page-5-0),[56,57](#page-7-0)} As discussed above, they were originally synthesized with oleate ligands, and the butyrate ligands were introduced through solution exchange. The high-frequency parts of the two spectra are shown in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S2. We find that as expected, the exchange of the oleate with the butyrate ligands is accompanied by a virtually complete disappearance of the 3000 cm^{-1} peak corresponding to the alkene C−H bond stretch. Additionally, both spectra confirm the lack of significant amounts of hydroxyl or protonated carboxylic acid groups in the sample (*cf.* ref [58](#page-7-0)).

In Figure 2b, we show the regions of the IR spectra of each film that contain the relevant carboxyl stretch frequencies. The

Figure 2. (a) Chemical structures of the considered ligands. (b) IR spectra of passivated PbS nanocrystals in the region of the ligand carboxyl stretches. For better comparison, the oleate data was offset vertically by 0.015. The 1380 and 1460 cm[−]¹ peaks in the butyrate spectrum assigned to impurities are indicated above (*).

spectrum of oleate-passivated PbS nanocrystals agrees very well with spectra previously reported in the literature.^{[9](#page-5-0),[21,22](#page-6-0),[37](#page-6-0),[59,60](#page-7-0)} We observe a symmetric C−O stretch peak at around 1400 cm[−]¹ followed by a band corresponding to C−H bends at around 1450 cm[−]¹ , and finally a broad and asymmetric peak between 1500 and 1560 cm^{-1} stemming from the antisymmetric C−O stretches. The progression of bands around and

below 1350 cm $^{-1}$ is known to correspond to CH₂ wagging and twisting modes.^{[23,](#page-6-0)[61](#page-7-0)} The spectrum of the butyrate-passivated nanocrystals features nearly identical line shapes and peak positions. The similarity of these spectra indicates that the oleate and butyrate ligands adopt very similar carboxylate binding geometries on the surface of the nanocrystal. We note, however, that unlike the oleate-passivated nanocrystals, the spectrum of the butyrate-passivated quantum dots is not stable. As shown in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S3, this evolution is associated with an increase in the intensity of the 1380 and 1460 cm[−]¹ peaks, indicated in Figure 2b, relative the those corresponding to the carboxyl stretches. We therefore speculate that these two features in the PbS:butyrate spectrum correspond to products of nanocrystal decomposition rather than the butyrate ligands passivating the nanocrystal surface. We note that although the line shape corresponding to these other entities (a set of two peaks at approximately 1380 and 1460 cm[−]¹) is typical of most alkane materials, we observe it also in films cast from chloroform, suggesting that the solvent per se is an unlikely source of these features, see [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S3.

Toy Model Simulations. We next move on to computational considerations. It is helpful to begin by studying a toy model system comprising a single butyrate ligand attached to a $Pb_{13}S_{12}I$ nanocrystal (the iodine atom was added to balance the charge/unpaired electrons without affecting the vibrational spectrum), see Figure 3a. Following the geometry optimization, the ligand relaxes to a "tilted-bridge"-type geometry with Pb−O bond lengths as indicated in panel (b). The IR spectrum calculated for this geometry using harmonic analysis is shown in Figure 3c and very broadly agrees with the experimental spectra of butyrate-capped nanocrystals and confirms the mode assignment discussed above. The model features a series of modes between 1200 and 1350 cm[−]¹ that can be assigned to CH_2 wagging and twisting modes, $\nu_{w/t}$. Around 1390 cm[−]¹ , we find the intense symmetric C−O stretch, ν_s , neighboring the much less intense umbrella mode of the methyl group, $\nu_{\rm w}$, which depending on the conformation can have a frequency above or below that of the symmetric C− O stretch. The mode around 1570 cm^{-1} corresponds to the antisymmetric C−O mode, ν _{as}. The above calculation also predicts a scissoring mode of the methylene group adjacent to the carboxylate, $\nu_{\rm sc}$ at around 1430 cm⁻¹. We note, however, that the calculated intensity of this mode is much weaker than that of the 1460 cm[−]¹ peak observed experimentally in the butyrate spectrum which we assigned to an impurity stemming from nanocrystal degradation. The remaining C−H bends, $ν_{\text{bend}}$, are similarly found to possess almost negligible IR intensities.

Figure 3. (a) Optimized structure of the toy model system, $Pb_{13}S_{12}I$:butyrate nanocrystal. (b) Optimized geometry of the butyrate ligand from (a). (c) Harmonic IR spectrum of the toy system with modes identified by inspection. See the text for a description of the vibrational mode labels.

In [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S3.1, we discuss the results of harmonic analyses performed on ten additional geometries obtained by optimizing different initial configurations, all of which relaxed into either bridging or tilted-bridging geometries. While the spectra remain qualitatively similar, we observe variations in IR intensities, vibrational frequencies, and the splitting Δ between the symmetric and antisymmetric C−O stretch frequencies. As shown in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S4, we find that the ν_{as} frequencies span a range of over 60 cm[−]¹ , while Δ varies between approximately 120-190 cm⁻¹.

Additionally, as discussed in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S3.2, we optimized the toy model system into a chelating geometry, although doing so required fixing the positions of the PbS atoms. The subsequent harmonic analysis yielded $\Delta \sim 130$ cm⁻¹. This suggests that different ligand binding modes can result in similar values of Δ , thereby limiting the utility of the commonly used rule-ofthumb for ligands that passivate nanocrystal surfaces.

ML-MD Simulations. Although the calculations performed on the toy system above appear to confirm the conventional mode assignment, they yield no information regarding the IR line shape or the underlying distribution of ligand geometries. Furthermore, the harmonic analysis does not capture possible anharmonic effects and, as discussed above, its results can be strongly conformation dependent. Finally, preferred ligand binding geometries may qualitatively differ on well-defined crystal facets and may change due to ligand−ligand interactions as the ligand density on the surface is increased.

To address these issues, we proceed to consider a more realistic, but still computationally tractable, model system, shown schematically in Figure 4. It comprises a small

Figure 4. Experimental and simulated IR spectra of butyratepassivated nanocrystals. Asterisks indicate peaks assigned to impurities. The simulated spectrum was obtained using Burg's maximum entropy spectral analysis method; 65 its comparison with the numerical Fourier transform result is shown in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S8. Inset: The $Pb_{19}S_6(butyrate)_{26}$ nanocrystal considered in the simulations.

octahedral nonstoichiometric $Pb_{19}S_6$ nanocrystal^{[10](#page-5-0)} passivated by 26 butyrate ligands, yielding the total system closed-shell and charge-neutral. Although the considered nanocrystal is significantly smaller than the ones used experimentally, in analogy to the experimentally used quantum dots, $10,56,57$ $10,56,57$ $10,56,57$ $10,56,57$ it possesses exclusively lead-rich (111) facets and should therefore support ligand binding geometries similar to those seen experimentally. We note that previous experimental studies of oleate-passivated PbS nanocrystals 21 found no significant dependence of the ligand IR spectra on the nanocrystal size (within the 2.9−4.9 nm diameter range),

suggesting that ligand geometries are largely unaffected by small variations in the ligand coverage density.

The IR spectrum for this system is obtained by considering the time-dependence of the total dipole moment during a constant-energy MD simulation. 62 To perform the necessary simulations, we trained a ML force field algorithm on DFT energies and forces; see [Methods](#page-1-0) for details. Additionally, we trained a ML algorithm to predict the total (DFT) dipole moment based on the atomic coordinates. The dipole vector is then calculated during a *NVE* simulation performed on a thermalized initial state (at $T = 300$ K). Finally, the IR signal is calculated from the dipole−dipole correlation function^o

$$
I(\omega) \propto \int_{-\infty}^{\infty} dt \langle \dot{\mu}(\tau)\dot{\mu}(t-\tau)\rangle_{\tau} e^{i\omega t}
$$
 (1)

where $\dot{\mu}(t)$ is the derivative of the dipole moment at time *t* and ⟨·⟩*^τ* denotes an ensemble average over *τ*. We note that the expression above already contains the harmonic quantum correction factor.^{[64](#page-7-0)}

The relevant region of the resulting spectrum is shown in Figure 4 (the spectrum over the entire frequency range is shown in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S7). It features two intense peaks corresponding to the symmetric and antisymmetric C−O stretches at around 1390 and 1520−1550 cm[−]¹ , respectively. Their relative positions, heights, and widths agree well with the experiment, to within the expected accuracy of DFT. (According to ref [66](#page-7-0) the B3LYP/6-31G* method yields an average error on predicted frequencies of roughly 36 cm^{-1} although this error can be significantly reduced when accounting for anharmonic effects as is done here.) This suggests that the simulations correctly capture the dynamics of the carboxylate ligands. The simulations also capture well the collective CH_2 vibrations (progression of bands between roughly 1200 and 1350 cm^{-1}). We note, however, that peaks previously assigned to impurities (around 1380 and 1460 cm[−]¹) are absent in the simulated spectrum. As we will demonstrate below, there exist C−H bending modes of frequencies between 1400 and 1500 cm^{-1} in the underlying nuclear dynamics. In agreement with the single-ligand calculations, however, their low intensities render them virtually silent. As we demonstrate in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S6, the very low intensities of the scissoring modes and the remaining C−H bends are independent of the used electronic structure method, further confirming our assignment of the 1460 cm^{-1} peak to impurities rather than a C−H bend within the surface butyrate ligands.

To further understand the simulated spectrum, we next calculate the vibrational densities of states (VDOS) for chemically distinct atom types from the individual atomic velocity correlation functions

$$
g_X(\omega) \propto \int_{-\infty}^{\infty} dt \sum_{n \in X} \langle \nu_n(\tau) \nu_n(t - \tau) \rangle_t e^{i\omega t}
$$
 (2)

where $v_n(t)$ is the velocity of atom *n* at time *t* and the sum runs over all chemically equivalent atoms of type *X*. VDOS for the oxygen and hydrogen atoms are plotted in [Figure](#page-4-0) 5a,b, respectively.

In the oxygen VDOS, as expected, we find two bands corresponding to the symmetric, ν_s , and antisymmetric C−O stretches, ν_{as} . In the case of the hydrogen atoms, in agreement with the single-ligand toy system, we find evidence of the methyl group umbrella modes, $\nu_{\rm w}$ overlapping with the

Figure 5. (a,b) VDOS for (a) oxygen and (b) hydrogen atoms calculated from a 100 ps *NVE* simulation.

symmetric C−O stretches. We can also confirm our assignment of the bands between 1200 and 1350 cm[−]¹ as predominantly CH₂ bending, $\nu_{w/t}$, although we note some oxygen contribution to vibrations in this frequency range. Finally, in the VDOS of the hydrogen atoms, there exists a clear peak at a frequency of roughly 1430 cm[−]¹ that corresponds to the previously discussed scissoring mode, *ν*_{sc}, as well as peaks corresponding to the remaining C−H bends, *ν*bend, *cf*. [Figure](#page-2-0) 3c. However, as discussed above and in [Section](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) [S6](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf), these modes are largely silent and, thus, virtually absent in the simulated IR spectrum.

Lastly, we investigate the geometries adopted by the butyrate ligands during the *NVE* simulation (and that therefore directly correspond to the observed IR spectrum). We use a method introduced in our previous study.^{[27](#page-6-0)} Briefly, for each ligand, we identify its primary lead atom, Pb*, as the lead atom closest to the average position of the two oxygen atoms. The two O−Pb^{*} distances are then defined as r_1 and r_2 , where r_2 > *r*₁. The shortest Pb−O distance from any other lead atom is defined as r_3 . In the case of the ligand shown in [Figure](#page-2-0) 3b, for

instance, we find $r_1 = 2.41$, $r_2 = 2.52$ and $r_3 = 2.80$ Å. The distance r_1 will generally correspond to that of a Pb−O (primarily ionic) bond. In the case of a chelating geometry, r_1 $\sim r_2$ and both are significantly shorter than r_3 . For a bridging ligand, on the other hand, the r_1 and r_3 distances should be comparable and shorter than r_2 . Finally, for a tilted-bridge, $r_1 \sim$ $r_2 \sim r_3$ while for a unidentate geometry, both r_2 and r_3 should be significantly longer than r_1 .

The results of the above analysis, the r_1 vs r_3 and r_2 vs r_3 histogram plots, are shown in Figure 6a,b. They reveal a very wide range of r_1 , r_2 , and r_3 values adopted by the ligands at room temperature in our simulations. Nonetheless, we observe a single maximum in both histograms, indicating that the tilted-bridge geometries dominate, although some amount of bridging ligands can also be found. This is in broad agreement with our earlier work on acetate-passivated nanocrystals, in which a different functional as well as a smaller basis set was used, suggesting that this result is largely independent of the chosen electronic structure method. Crucially, although the absorption band corresponding to the antisymmetric C−O stretches possesses a highly non-Lorentzian structure, we find no evidence for the existence of significant numbers of chelating geometries or, in fact, for a bimodal distribution of ligand geometries of any type. Instead, this asymmetric and seemingly structured spectrum appears to arise due to an inherently broad and asymmetric distribution of (largely) tilted-bridge geometries. The highly disordered nature of the nanocrystal−ligand interface implies that the experimental C− O stretch bands cannot be interpreted simply as a sum of the peaks corresponding to distinct coordination types. This is especially true given that, as shown in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf) S4, the conformation of carboxylate ligands on the nanocrystal surface affects not only the C−O stretch frequencies but also their corresponding intensities.

■ **CONCLUSIONS**
In summary, we studied the experimental vibrational spectra of oleate- and butyrate-passivated PbS nanocrystals and demonstrated that these two ligands possess very similar binding geometries. This allowed us to study the computationally more expedient butyrate ligands in lieu of the oleate ligands customarily used experimentally to enhance the stability of colloidal nanocrystals. We first considered a single-ligand toy system, which allowed for a straightforward mode assignment through harmonic mode analysis. We then investigated a more realistic model comprising a small octahedral PbS nanocrystal

[Figure](#page-3-0) 6. Histograms showing (a) r_1 vs r_3 and (b) r_2 vs r_3 values adopted during the *NVE* simulation used to obtain the IR spectrum in Figure 4.

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Notes

The authors declare no competing financial interest.

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passivated by twenty-six butyrate ligands. The corresponding IR spectrum was obtained from an MD simulation performed with a machine-learned force field trained on DFT data. We obtained good agreement with the experimental spectrum and therefore confirmed that ML-AIMD simulations constitute an effective tool in modeling the IR response of nanoscopic systems.

Our work also resolves the apparent inconsistency between the conventional interpretation of the IR spectroscopy of carboxylate-passivated PbS nanocrystals^{18,[21](#page-6-0)–[23](#page-6-0),[37](#page-6-0)} and previous computational studies on these systems.[27](#page-6-0) The former postulated a coexistence of bridging and chelating ligand geometries, while the latter suggested that chelating geometries should not be observed. Our simulations indicate that the experimental IR line shape can result from a broad distribution of tilted-bridge geometries. Importantly, this work illustrates the limitations of interpreting nanocrystal IR spectra based on empirical rules derived from studies of metal complexes since the wide range of conformations accessible to carboxylate ligands can result in broad and non-Lorentzian IR line shapes even if few nominal coordination types are present on a nanocrystal's surface.

■ **ASSOCIATED CONTENT**

Data Availability Statement

The data that support the findings of this study are openly available at the following URL: [https://figshare.com/articles/](https://figshare.com/articles/dataset/Simulations_of_IR_spectroscopy_of_PbS_nanocrystals/25236574) [dataset/Simulations_of_IR_spectroscopy_of_PbS_](https://figshare.com/articles/dataset/Simulations_of_IR_spectroscopy_of_PbS_nanocrystals/25236574) [nanocrystals/25236574.](https://figshare.com/articles/dataset/Simulations_of_IR_spectroscopy_of_PbS_nanocrystals/25236574)

\bullet Supporting Information

The Supporting Information is available free of charge at [https://pubs.acs.org/doi/10.1021/acs.jpcc.4c01988.](https://pubs.acs.org/doi/10.1021/acs.jpcc.4c01988?goto=supporting-info)

> Details of the experimental procedure and additional experimental results; details of the ML training procedure; additional toy-model results; additional ML-MD results; discussion regarding the C−H bending mode intensity; simulation results obtained using the smaller-basis-set force field ([PDF](https://pubs.acs.org/doi/suppl/10.1021/acs.jpcc.4c01988/suppl_file/jp4c01988_si_001.pdf))

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